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## APPROXIMATE METHODS FOR CENTER OF PRESSURE PREDICTION OF MULTI-SEGMENT WINGS



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#### 14. ABSTRACT (Maximum 200 Words)

Approximate methods for predicting the center of pressure of multi-segment wings are presented. Only wings with breaks in the leading edge sweep are considered. The methods transform a multi-segment planform into an equivalent straight tapered planform. Comparisons are made with predictions from a vortex lattice code and experimental data at subsonic speeds and with predictions from a vortex lattice and an Euler code at supersonic speeds. The most accurate method studied had an average error in predicted center of pressure location of approximately 2 percent of the root chord.

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# Approximate Methods for Center of Pressure Prediction of Multi-Segment Wings

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#### **ABSTRACT**

Approximate methods for predicting the center of pressure of multi-segment wings are presented. Only wings with breaks in the leading edge sweep are The methods transform a multi-segment considered. planform into an equivalent straight tapered planform. Comparisons are made with predictions from a vortex lattice code and experimental data at subsonic speeds and with predictions from a vortex lattice and an Euler code at supersonic speeds. The most accurate method studied had an average error in predicted center of pressure location of approximately two percent of the root chord.

## LIST OF SYMBOLS

angle of attack α aspect ratio, b2/S AR

wing span b

pitching moment coef., (pitching moment/q..Scr)  $C_{m}$ 

normal force coef., (normal force/q...S)  $C_N$ 

root chord  $c_r$ 

tip chord  $C_{t}$ 

sweep angle Λ

lateral position of break in sweep angle, y/(b/2) η

taper ratio (c<sub>r</sub>/c<sub>t</sub>) λ

dynamic pressure q∞

Reynold's number RN

wing area S

center of pressure, measured aft of apex x<sub>cp</sub>

center of pressure, measured aft of apex, x<sub>cp</sub> **XCP** 

area centroid, measured aft of apex xcent

#### Subscripts

leading edge LE

trailing edge TE

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### INTRODUCTION

Typical tactical missiles have fins with small chord lengths relative to the overall body length. As a result, static stability and trim are not significantly affected by errors in the predicted center of pressure of these fins. Many high-speed vehicles, however, employ very highly swept strakes on the inboard portion of the wing. In some cases, the strakes are so large that the root chord of the wing is as long as the fuselage. The stability and trim of these configurations are much more sensitive to errors in the predicted wing center of pressure.

Preliminary aerodynamic design codes such as Missile Datcom (Ref. 1) and the Naval Surface Warfare Center AP98 (Ref. 2) use approximate methods to model straked wings. Given a straked wing geometry, they define an equivalent straight tapered wing which is used for the subsequent analysis. Spencer (Ref. 3) showed that the equivalent wing method can produce excellent subsonic lift predictions if the appropriate algorithm is used to define the equivalent straight tapered wing. However, he did not extend his analysis to include supersonic speeds or consider center of pressure predictions.

The algorithm used for multi-segment wing center of pressure (x<sub>cp</sub>) calculations in the 8/99 version of Missile Datcom has been found to be inadequate when compared with data from future generation reusable launch vehicles with long strakes such as the X-34 and X-37 shown in Figure 1. The objective of this effort was to identify an alternative transformation methodology for yielding improved x<sub>cp</sub> predictions for multi-segment wings at small angles of attack suitable for inclusion into a future release of Missile Datcom. Only planforms with a break in the leading edge sweep were considered. Planforms with breaks in the trailing edge will be studied in a subsequent effort.

## TECHNICAL APPROACH

The problem of developing an algorithm for multisegment wing center of pressure calculations can be divided into two distinct parts: (1) defining the equivalent planform geometry and (2) placing the center of pressure determined from the equivalent planform onto the actual planform. For this study, nine methods for defining the equivalent planform geometry were analyzed and three methods for placing the center of pressure onto the segmented planform were considered. Details concerning each of the methods evaluated as part of this investigation are presented next followed by a discussion of the approach used for their evaluation.

## **Transformation Methods**

Missile Datcom computes the center of pressure of a wing using design charts which are a function of aspect ratio, taper ratio, leading edge sweep angle and Mach number. All of the transformation methods investigated held constant the total area (S), span (b/2), and aspect ratio (AR) of the original planform, while allowing other aspects of the wing geometry to vary. For purposes of convenience and comparison, the equations used for each of the transformation methods are provided in Table 1. A more formal derivation of these equations follows.

#### Method A

The wing transformation approach used for center of pressure calculations at all speeds in the 8/99 version of Missile Datcom is denoted as Method A. Missile Datcom also uses this method to compute the normal force slope of multi-segment wings at supersonic speeds. The method evaluates a segmented planform by transforming the planform into a straight-tapered approximation with the same taper ratio as the original planform and defines an effective leading edge sweep angle based on the areaweighted average of the leading edge sweep angles of each segment, using:

$$\Lambda_{LE} = \frac{1}{S} \left[ \sum \Lambda_{LE,i} S_i \right] \tag{1}$$

where  $(\Lambda_{LE,i})$  and  $S_i$  define the leading edge sweep angle and planform area of each wing segment, respectively. The root chord of the transformed wing is calculated using:

$$c_r = \frac{2S}{b(1+\lambda)} \tag{2}$$

Method A calculates the  $x_{cp}$  of the transformed wing using a proportional method that preserves the location of the  $x_{cp}$  as a percentage of the root chord as follows:

$$\left(\frac{x_{cp}}{c_r}\right) = \left(\frac{x_{cp}}{c_r}\right)_{\text{effective}} \tag{3}$$

#### Method B

Method B uses the transformation developed by Spencer for wings at subsonic speeds, Ref. 3. Missile Datcom uses this method to compute the normal force slope of multi-segment wings at subsonic speeds. It computes an effective mid-chord sweep angle ( $\Lambda_{c/2}$ ) using an areaweighted average:

$$\Lambda_{c/2} = \cos^{-1} \left[ \frac{1}{S} \Sigma \cos \Lambda_{c/2,i} S_i \right]$$
 (4)

This is then used to calculate the effective leading edge sweep angle using:

$$\Lambda_{LE} = \tan^{-1} \left[ \tan \Lambda_{c/2} + \frac{2(1-\lambda)}{AR(1+\lambda)} \right]$$
 (5)

Like Method A, Method B maintains the taper ratio of the original wing and uses the proportional placement approach provided by Equation 3 to translate the  $x_{cp}$  of the transformed fin onto the original fin.

#### Method C

Method C is a variation of Method B that uses the midchord sweep angle rather than the cosine of the angle to calculate the effective sweep:

$$\Lambda_{c/2} = \frac{1}{S} \sum \Lambda_{c/2,i} S_i$$
 (6)

Like the two preceding methods, this method maintains the taper ratio of the original wing and locates the  $x_{cp}$  of the segmented planform proportionally according to Equation 3.

#### Method D

Method D (Ref. 4) differs significantly from the previous methods in that it holds constant the trailing edge sweep angle and tip chord of the original planform to define a straight-tapered panel, and allows the taper ratio to vary.

The effective leading edge sweep angle based on the trailing edge sweep, aspect ratio, and taper ratio of the original planform is calculated using:

$$\Lambda_{LE} = \tan^{-1} \left[ \tan \Lambda_{TE} + \frac{4}{AR} \frac{(1-\lambda)}{(1+\lambda)} \right]$$
 (7)

The effective root chord of the planform is computed using:

$$c_r = \frac{2S}{b} - c_t \tag{8}$$

This method also uses a different procedure to translate the  $x_{cp}$  of the transformed wing back onto the original planform. Rather than placing the  $x_{cp}$  proportionally, as the previous methods do, Method D lines up the trailing edges of the segmented and straight-tapered planforms, and places the  $x_{cp}$  of the original planform at the same distance from the trailing edge as the  $x_{cp}$  of the transformed planform. This realignment of the  $x_{cp}$  from the transformed wing to the original wing can be performed using:

$$\left(\frac{x_{cp}}{c_r}\right) = 1 - \left[1 - \left(\frac{x_{cp}}{c_r}\right)_{effective}\right] \frac{c_{r,effective}}{c_r} \tag{9}$$

#### Method E

Method E is a variation of Method D that maintains the taper ratio of the original planform rather than the tip chord. It also uses the same aft  $x_{cp}$  trailing edge alignment method as Method D (Equation 9).

Both Methods D and E could be extended to planforms with breaks in the trailing edge sweep angle by using:

$$\Lambda_{TE} = \frac{1}{S} \Sigma \Lambda_{TE,i} S_i \tag{10}$$

#### Method F

A hybrid method, denoted as Method F, combines approaches used in Methods A and D. Like Method A, this method uses Equation 1 to calculate an effective leading edge sweep angle and uses the proportional placement approach defined in Equation 2 for locating  $x_{cp}$ . However, the tip chord of the original planform is held constant, as is done for Method D.

#### Method G

The equivalent tangent leading edge sweep method, denoted as Method G, maintains the same geometric properties and uses the same  $x_{cp}$  placement method as Method A; however, it uses the tangents of the segmented wing leading edge sweep angles to determine an effective leading edge sweep angle using:

$$\Lambda_{LE} = \tan^{-1} \left[ \frac{1}{S} \sum \tan \Lambda_{LE,i} S_i \right]$$
 (11)

#### Method H

Method H, obtained from Reference 2, is one of two wing transformation methods contained the AP98 aerodynamic prediction code. The method holds constant both the inboard leading edge sweep angle and the trailing edge sweep angle of the original planform, and uses the equations below to calculate new root and tip chords, respectively.

$$c_r = \left[\frac{S}{b} - \frac{b}{4} \left( \tan \Lambda_{TE} - \tan \Lambda_{LE} \right) \right]$$
 (12)

$$c_t = \left[ \frac{S}{b} + \frac{b}{4} \left( \tan \Lambda_{TE} - \tan \Lambda_{LE} \right) \right]$$
 (13)

For configurations where the inboard section of the wing is highly swept, such as with strakes, these equations can yield negative tip chords. This method was not evaluated where a negative value for tip chord was obtained in this study. However, AP98 assigns a tip chord of zero and calculates a new root chord in these cases.

The  $x_{cp}$  placement approach that AP98 uses lines up the area centroids of the original and transformed wings and places the  $x_{cp}$  of the segmented wing the same distance from the centroid as is the  $x_{cp}$  of the straight-tapered wing, using:

$$\left(\frac{x_{cp}}{c_r}\right) = \left(\frac{x_{cent}}{c_r}\right) + \frac{c_{r,effective}}{c_r} \left(\frac{x_{cp} - x_{cent}}{c_r}\right)_{effective} \tag{14}$$

#### Method I

The second method used by AP98, denoted as Method I, maintains the inboard leading edge sweep angle of the

original planform as is done for Method H. However, Method I maintains the taper ratio of the original planform and allows the trailing edge sweep angle to vary. It uses the area centroid placement approach used by Method H to locate the  $x_{cp}$  of the segmented wing.

#### **Evaluation Approach**

An extensive literature search was performed to locate experimental data suitable for further evaluation and validation of the most promising wing transformation approaches. Unfortunately, very little data for isolated wings is available, and what little was identified exists only at subsonic speeds. In order to perform as systematic evaluation of the accuracy of the various transformation methods, fourteen segmented planforms were defined to represent a broad range of reusable launch vehicle and missile fin designs. Referring to Figure 2, the wing geometric parameters varied for this study included: inboard and outboard leading edge sweep angle, trailing edge sweep angle, taper ratio, and spanwise location of the sweep break. The span of the planforms was held constant. Table 2 lists the design parameters of the segmented planforms investigated. Corresponding scaled drawings of these wings are provided in Figure 3.

Each of the segmented planform designs was converted into equivalent straight tapered planforms using the nine wing transformation methods previously described. These configurations were analyzed with Missile Datcom at Mach numbers of 0.3, 2.0, and 4.0 to obtain a set of  $C_m$  and  $C_N$  predictions from which an  $x_{cp}$  prediction (defined in terms of root chord percentage) was calculated as:

$$\frac{x_{cp}}{c_r} = -\frac{C_m}{C_N} \qquad (@ \alpha = 4 \text{ deg})$$
 (15)

In order to determine which of the methods examined was most accurate, comparisons were made between Missile Datcom results, obtained on each of the transformed straight tapered planforms, and "exact" analytical solutions, obtained for each original multi-segmented using the vortex lattice code HASC (Reference). The HASC analysis was performed at the same Mach numbers and angles of attack as the Missile Datcom analysis. The Missile Datcom results for all of the transformed wings assumed proportional placement for  $x_{cp}$  (Eq. 3). These were post-processed to give trailing edge placement for Methods D and E and centroid placement for Methods H and I.

To address numerical uncertainty issues associated with the placement and density of the bound vortices modeled in HASC, a parametric sensitivity study was performed by varying the number of chordwise and spanwise bound vortices for a limited set of both multi-sweep and straight-tapered wing geometries for which experimental data were available. Results from this study were used as a guide for the vortex distributions applied on each of the fourteen multi-segmented planforms evaluated. The distributions used for assessing the Missile Datcom results were sufficient to limit numeric difference associated with the vortex distributions to less than 0.1% of the calculated  $x_{\rm cp}/c_{\rm r}$  value.

As an additional check of the validity of using HASC to perform this evaluation, three of the multi-segment planforms (Configurations 1, 3, and 13) were analyzed using the space-marching Euler code ZEUS (Ref. 6). These results were compared with the HASC results for  $x_{cp}/c_r$  at Mach 2 and 4 and found to be within 1 percent of one another at a four-degree angle of attack.

All predicted results obtained for this investigation (Missile Datcom, HASC, and ZEUS) were independent of Reynold's number and assumed infinitely thin cross sections. Sign conventions used for the analysis are shown in Figure 4.

## **RESULTS AND ANALYSIS**

Table 3 provides a summary of the average error in center of pressure location, as a fraction of the root chord length, for each of the nine methods considered at Mach 0.3, 2.0 and 4.0. The percent error is defined as the percent difference between the results obtained using the various transformation methods and the "exact" solutions obtained from HASC. Methods D and E are clearly superior to the other methods with average errors on the order of 1/4 or less of those obtained using the transformation method used in the 8/99 version of Missile Datcom (Method A). With only one exception, all of the methods investigated provided greater accuracy than Method A. As noted above, the data reduction procedure generated proportional x<sub>cp</sub> placement results for the planforms generated by Methods D, E, H and I. These were inferior to the desired placement results in all cases.

Figure 5 plots the percent error in wing x<sub>cp</sub> versus wing aspect ratio for each of the 14 segmented wings investigated at Mach 0.3, 2.0 and 4.0, respectively. In addition to the results obtained from Method A, results for Methods B, C, D and E are also included. The number of methods shown on these figures was limited to the most promising transformation approaches, in order to facilitate clear comparisons between them.

Inspection of Figure 4 shows that the errors associated with Method A are frequently greater than 10 percent at Mach 0.3 and 2.0 for wing aspect ratios less than 1.2. Methods D and E have the lowest percent errors and yield very similar results for all configurations. exception of the lowest aspect ratio wings (configurations 10 and 11), the x<sub>cp</sub> percent error for Methods D and E is less than 5 percent for all wings at both Mach 0.3 and 2.0. The close agreement in results is not surprising given the similarity of the two methods. At Mach 4.0, all methods demonstrated greater accuracy, but the overall trends observed remained consistent with those observed at Mach 0.3 and 2.0. The x<sub>cp</sub> percent error for Methods D and E were both less than 5 percent for all configurations evaluated at Mach 4.0.

Methods A and E were compared with a limited set of subsonic experimental data obtained References 7 through 11 to validate the assessments made from comparisons with "exact" solutions generated by HASC. Table 4 identifies the wing configurations and test conditions for which subsonic experimental data was obtained for Figure 6 provides the scaled validation purposes. planform views of each of the wings identified in Table 4. A plot comparing x<sub>cp</sub> percent error as a function of aspect ratio for both Methods A and E is shown in Figure 7. As observed in "exact" data comparisons made in Figure 5, Method E x<sub>cp</sub> predictions are consistently within five percent of the experimental data, while Method A xcp errors are anywhere from two to five times greater than Method E. The maximum error for the experimental x<sub>cp</sub> data is estimated to be within one percent of the wing root chord.

The values of center of pressure discussed thus far are only used by Missile Datcom for the linear lift contribution, i.e., at low angles of attack. Missile Datcom uses the wing centroid as the center of pressure for the non-linear lift contribution. The overall wing  $x_{cp}$  is computed using:

$$\frac{x_{cp}}{c_r} = \frac{C_{N,linear}(x_{cp}/c_r) + C_{N,non-linear}(x_{cent}/c_r)}{C_N}$$
 (16)

To assess the performance of Method E relative to Method A in Missile Datcom, plots of  $x_{cp}/c_r$  were generated versus angle of attack for wing configurations 15, 16, 17, 22 and 23. These plots are presented in Figures 8 through 12 in numeric order. Method E yields significantly better yields results than Method A for all four configurations and Method E is within four percent of experimental x<sub>cp</sub>/c<sub>r</sub> values for angles of attack up to 25 degrees.

## SUMMARY AND CONCLUSIONS

The results of this study have shown that several transformation methods are superior to the method contained in the 8/99 version of Missile Datcom. The independent validation of findings from the "exact" solutions study, obtained through the use of experimental data, has confirmed that the incorporation of Method E Missile Datcom will result in significant improvements to the capability of the code to predict the x<sub>cp</sub> of multi-segmented wings at subsonic speeds. It is also reasonable to assume that, based on the results of the "exact" study, Method E will also yield significant improvements for supersonic predictions.

Due to the inability to predict "exact" analytical solutions and the lack of experimental data, no conclusions can be drawn for the transonic flight regime. There is clearly a need to obtain experimental data for validating Method E at supersonic transonic speeds.

The next release of Missile Datcom (Version 9/02) will incorporate Method E for predicting the x<sub>cp</sub> of multisegmented wings. This improvement will be of particular benefit for the aerodynamic assessment of reusable launch vehicle design concepts as well as unconventional missile fin designs.

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Table 1. Summary of Transformation Methods for Multi-Segment Wings

Method	Maintains	$\Lambda_{ t LE}$	
A (Ref 1)	b, S, λ	$\frac{1}{S}\sum \Lambda_{LE,i}S_{i}$	2S
B (Ref 3)	b, S, A	$\tan^{-1}\left[\tan\Lambda_{c/2} + \frac{2(1-\lambda)}{AR(1+\lambda)}\right], \cos\Lambda_{c/2} = \frac{1}{S}\sum\cos\Lambda_{c/2,i}S_{i}$	$\frac{b(1+\lambda)}{2S}$ $\frac{2S}{b(1+\lambda)}$
С	b, S, λ	$\tan^{-1}\left[\tan\Lambda_{c/2} + \frac{2(1-\lambda)}{AR(1+\lambda)}\right], \Lambda_{c/2} = \frac{1}{S}\sum\Lambda_{c/2,i}S_i$	$\frac{2S}{b(1+\lambda)}$
D (Ref 4)	b, S, A <sub>TE</sub> , C <sub>T</sub>	$\tan^{-1}\left[\tan\Lambda_{TE} + \frac{4(1-\lambda)}{AR(1+\lambda)}\right]$	$\frac{2S}{b} - C_T$
E	b, S, Λ <sub>ΤΕ</sub> λ	$\tan^{-1}\left[\tan\Lambda_{TE} + \frac{4(1-\lambda)}{AR(1+\lambda)}\right]$	$\frac{2S}{b(1+\lambda)}$
F	b, S, C <sub>T</sub>	$\frac{1}{S}\sum_{i}\Lambda_{LE,i}S_{i}$	$\frac{2S}{b} - C_T$
G	b, S, λ	$\tan^{-1} \left[ \frac{1}{S} \sum \tan \Lambda_{LE,i} S_i \right]$	
H Ref 2)	b, S, Λ <sub>LE,1</sub> , Λ <sub>TE,1</sub>	$\Lambda_{LE,1}$	$b(1+\lambda)$ $2S$
I Ref 2)	b, S, Λ <sub>LE,1</sub> λ	$\Lambda_{LE,1}$	$\frac{b(1+\lambda)}{\frac{S}{b} - \frac{b}{4} (\tan \Lambda_{TE} - \tan \Lambda_{LE})}$

Table 2. Fin Geometries for Systematic Investigation

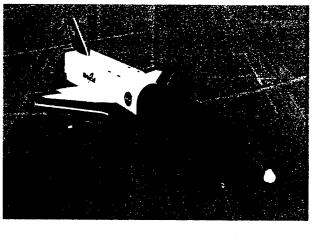
Fin	Λ <sub>LE</sub> ,	Λ <sub>LE,2</sub>	Λ <sub>TE</sub>	λ	η	AR
1	80	0	0	0.25	0.5	1.22
2	80	40	-40	0.25	0.5	0.72
3	80	40	-20	0.25	0.5	0.84
4	80	40	0	0.25	0.5	0.94
5	80	40	20	0.25	0.5	1.10
6	80	40	40	0.25	0.5	1.42
7	80	40	-20	0.25	0.25	1.28
8	80	40	0	0.25	0.25	1.60
9	80	40	20	0.25	0.25	2.1
10	80	40	0	0.25	0.5	0.56
11	0	80	0	0.5	0.5	0.40
12	40	0	0	0.5	0.5	3.82
13	0	40	0	0.5	0.5	2.72
14	0	40	0	0.25	0.25	3.32

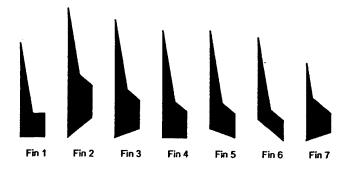
Table 3. Average Error in Predicted  $x_{cp}$ 

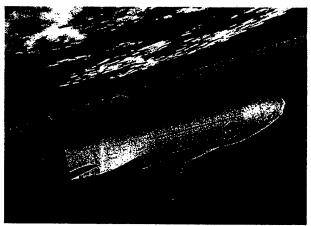
Method	M = 0.3	M = 2.0	M = 4.0
A	12.2	11.0	7.5
В	5.9	6.0	3.3
C	8.6	7.8	4.2
D	2.6	3.3	1.8
Е	2.3	2.8	1.1
F	8.2	8.1	6.0
G	13.5	12.3	13.3
Н	9.5	9.6	6.0
· I	7.7	9.3	6.0

Table 4. Fin Geometries Used for Validation

Fin	Λ <sub>LE,1</sub>	Λ <sub>LE,2</sub>	Λ <sub>TE</sub>	λ	η	AR	Mach	RN (ft -1)	Ref.
15	80	30	-30	0	0.17	3.08	0.14	$1.0 \times 10^6$	7
16	80	40	-40	0	0.17	2.16	0.14	$1.0 \times 10^6$	7
17	70	47.5	-47.5	0	0.39	1.64	0.14	1.0 x 10 <sup>6</sup>	7
18	73	47.2	0	0	0.56	1.76	0.40	2.5 x 10 <sup>6</sup>	8
19	73	47	0	0.29	0.56	1.6	0.40	2.5 x 10 <sup>6</sup>	8
20	73	0	0	0.29	0.56	1.76	0.40	2.5 x 10 <sup>6</sup>	8
21	60	25	2	0.09	0.38	5.10	0.50	0.9 x 10 <sup>6</sup>	9
22	76	40	0	0.15	0.26	2.42	0.23	1.7 x 10 <sup>6</sup>	10
23	80	65	0	0	0.37	1.60	<0.2	-	11







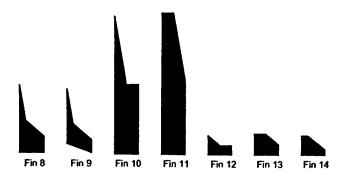
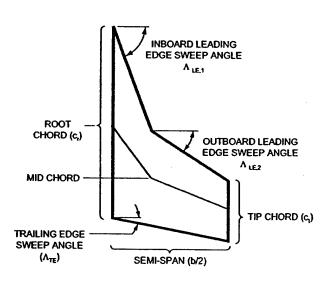


Figure 3. Wing Planforms Used for Analytic Study.

Figure 1. Photographs of X-34 and X-37.



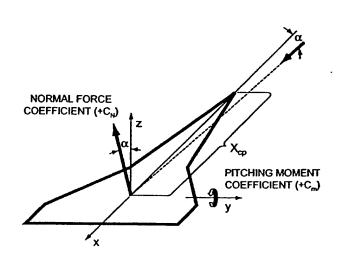


Figure 4. Sign Conventions.

Figure 2. Wing Parameters.

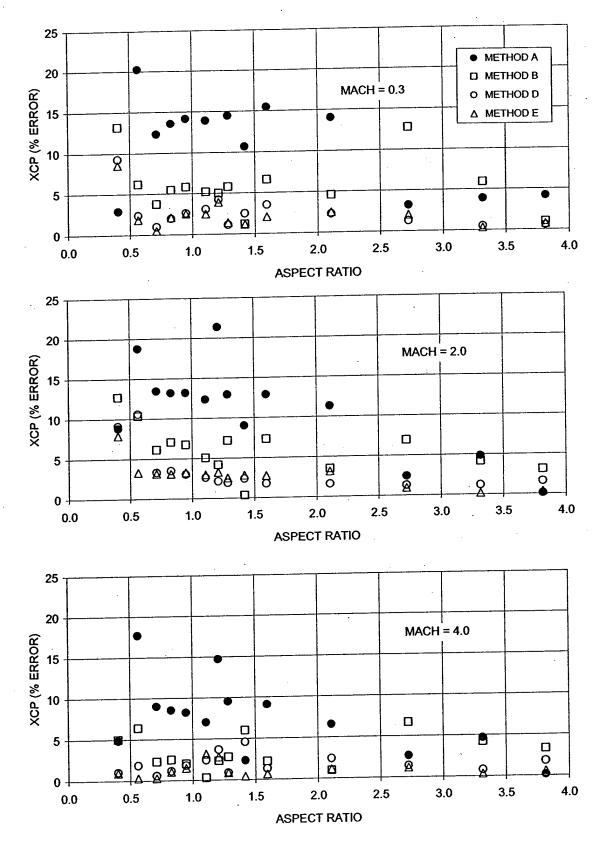


Figure 5. Analytical Error Versus Aspect Ratio.

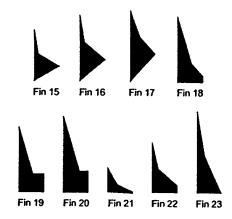


Figure 6. Wing Planforms Used for Validation.

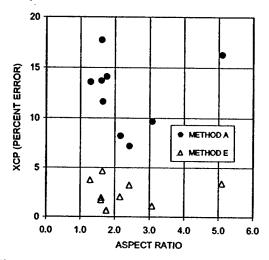


Figure 7. Experimental Error Versus Aspect Ratio.

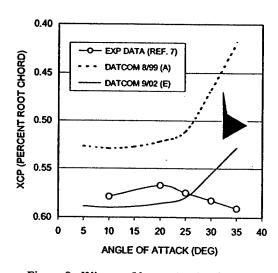


Figure 8. Wing x<sub>cp</sub> Versus Angle of Attack, Configuration 15, Mach = 0.14.

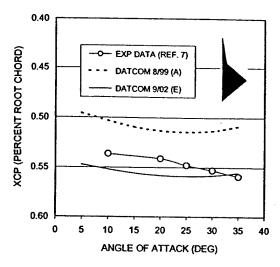


Figure 9. Wing x<sub>cp</sub> Versus Angle of Attack, Configuration 16, Mach = 0.14.

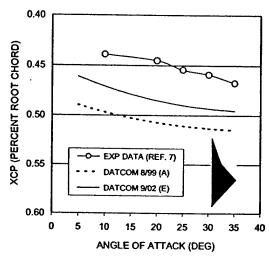


Figure 10. Wing x<sub>cp</sub> Versus Angle of Attack, Configuration 17, Mach = 0.14.

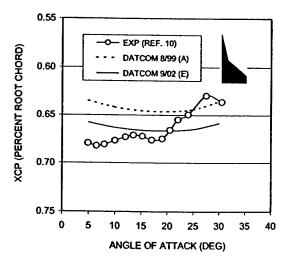


Figure 12. Wing x<sub>cp</sub> Versus Angle of Attack, Configuration 22, Mach = 0.23.

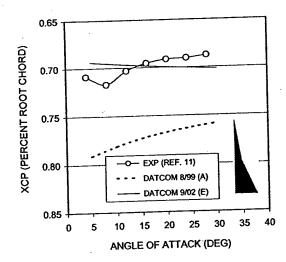


Figure 13. Wing x<sub>cp</sub> Versus Angle of Attack, Configuration 23, Mach < 0.2.